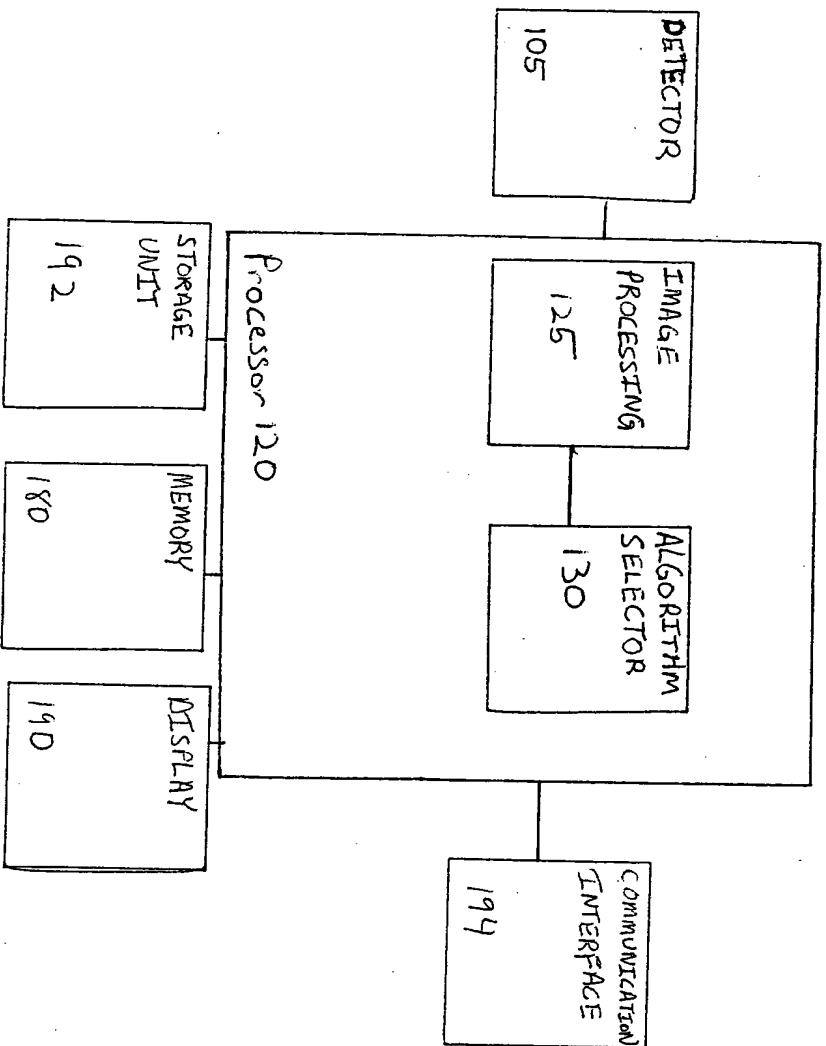


FIG 1



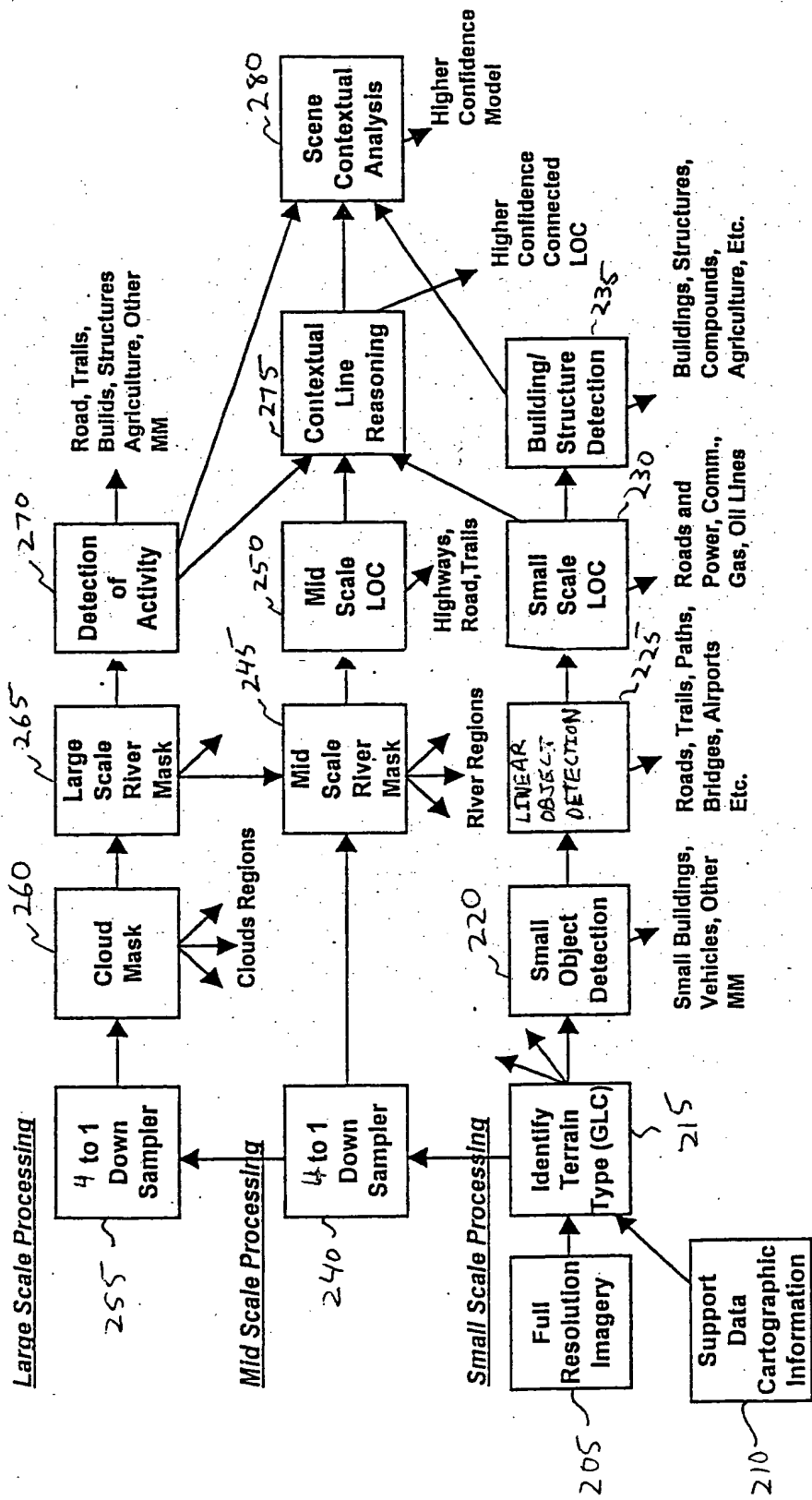


FIG 2

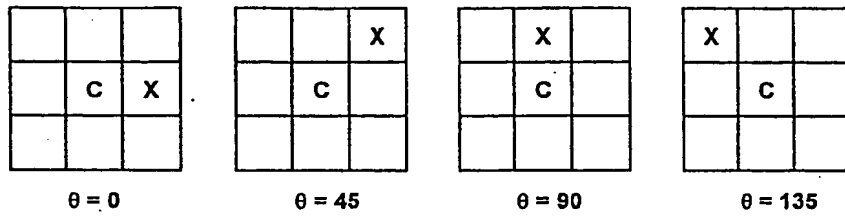


FIG 3

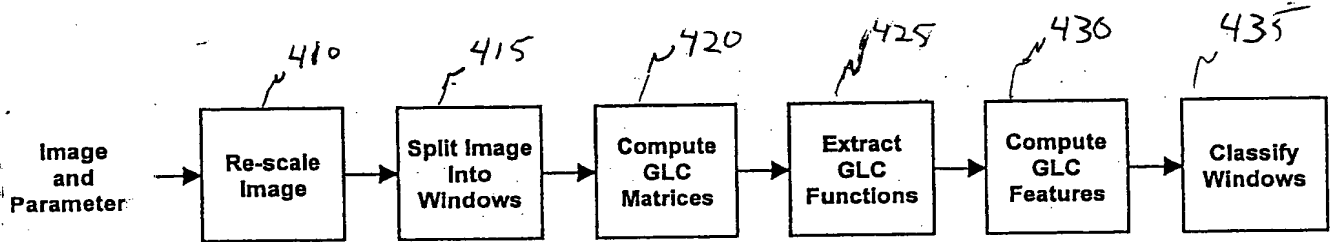


FIG. 4

Energy

$$E_n = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j))^2$$

Entropy

$$E_t = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j) \log(G(i, j)))$$

Contrast

$$C_t = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j) \times (i - j)^2)$$

Inverse_Difference_Moment

$$E_n = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} \frac{G(i, j)}{1 + (i - j)^2}$$

Correlation

$$C_r = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} \frac{i \times j \times G(i, j) - \mu_x \times \mu_y}{\sigma_x \times \sigma_y}$$

FIG 5

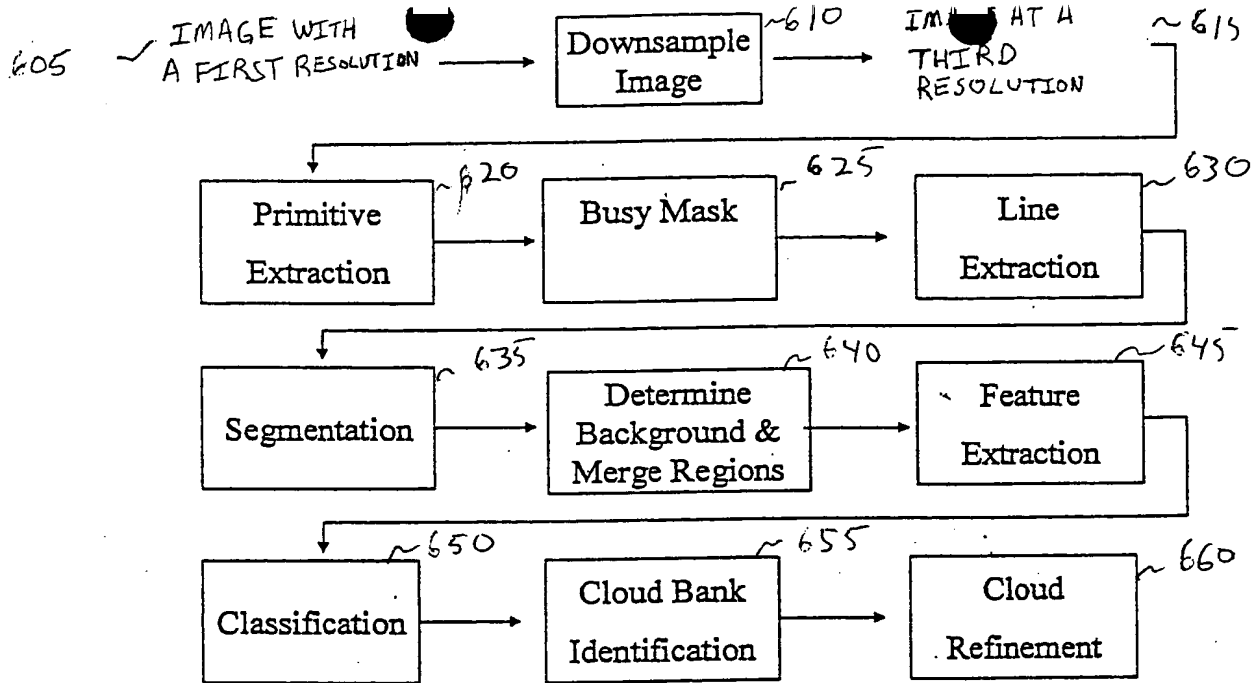
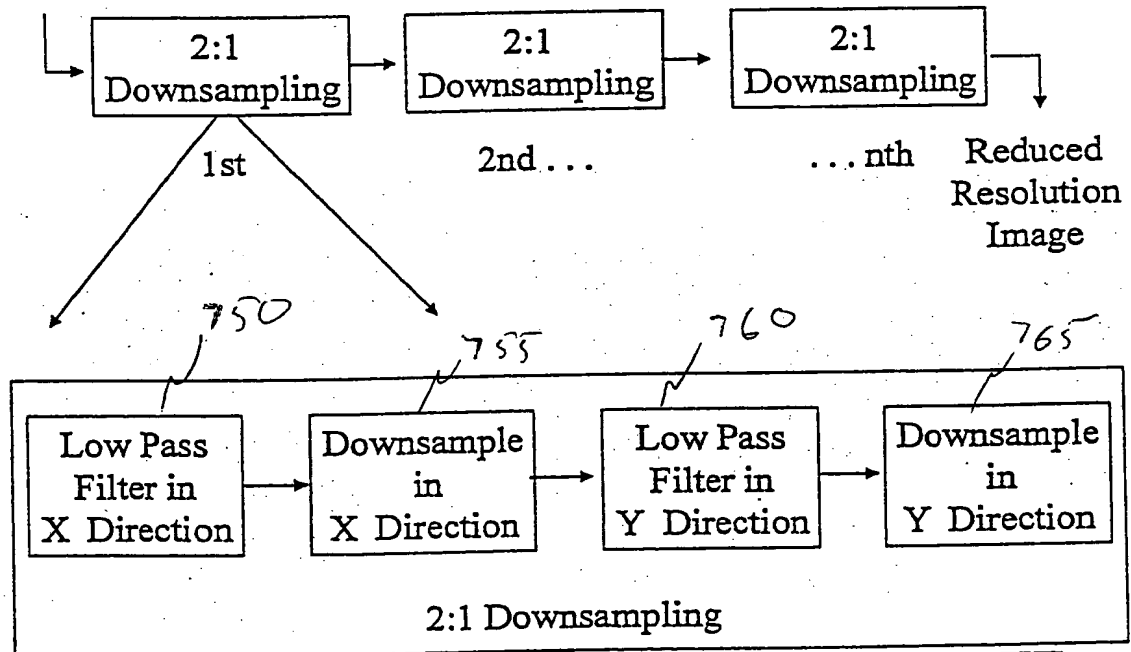


FIG 6

IMAGE WITH A FIRST RESOLUTION

FIG 7A



1	4	6	4	1
1	16	24	16	1
1	24	36	24	1
1	16	24	16	1
1	4	6	4	1

Full 6 by 6 Convolution Filter

FIG 7B

1	4	6	4	1
---	---	---	---	---

X Direction Filter

FIG 7C

1
4
6
4
1

Y Direction Filter

FIG 7D

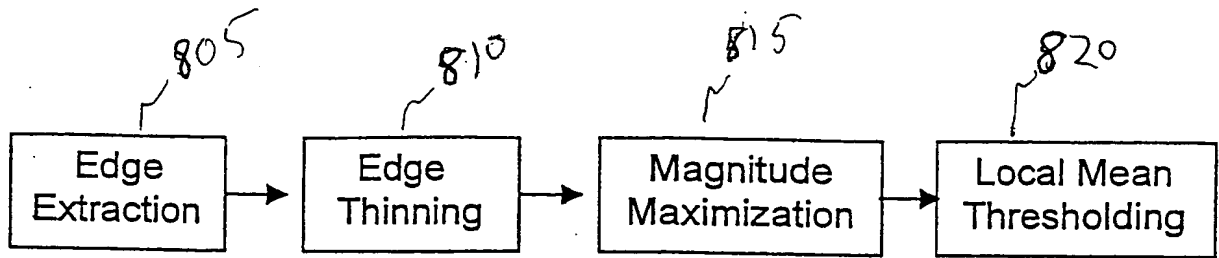


FIG 8

-1 -2 -1	-1 0 1	4 5 6
0 0 0	-2 0 2	3 * 7
1 2 1	-1 0 1	2 1 8
Horizontal Component Template	Vertical Component Template	Directional Mapping

D_x = convolution of the vertical template with the image

D_y = convolution of the horizontal template with the image

$$\text{Sobel Magnitude} = (D_x^2 + D_y^2)^{1/2}$$

Sobel Direction = $\text{Arctan} (D_y / D_x)$ mapped to 8 directions

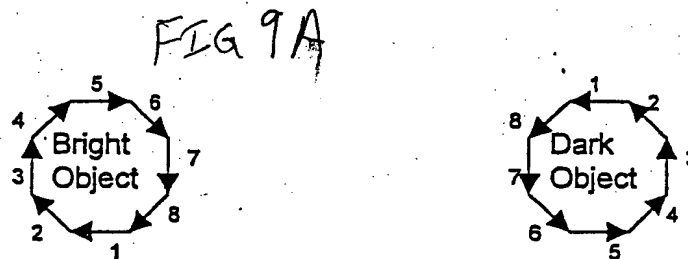


FIG 9B

<u>Directions 3 & 7</u>	<u>Directions 1 & 5</u>	<u>Directions 2 & 6</u>	<u>Directions 4 & 8</u>
O O O O O	O X X X O	O O O X O	O X O O O
X O O O X	O O X O O	O O O X X	X X O O O
X X C X X	O O C O O	O O C O O	O O C O O
X O O O X	O O X O O	X X O O O	O O O X X
O O O O O	O X X X O	O X O O O	O O O X O

C = Center pixel X = Non-zero pixel O = Don't care pixel

FIG 10

```

      XXX
     XXXXX
    XXXXXX
   XXXXXX
  XXXXXX
 XXXXX
XXXX
XXXX

```

FIG 11A

```

      XXX
     XXX
    XXX
   XXX
  XXX
 XXX
XX

```

FIG 11B

X1X	X1X	XXO	OXX
XC1	1CX	1CX	XC1
OXX	XXO	X1X	X1X

1 = non-zero pixel, o = zero pixel, x = don't care

FIG 12

```

      XXX
     XXX
    XXX
   XXX
  XXX
 XXX
XX

```

FIG 13A

```

      XX
     XX
    XX
   XX
  XX
 XX
XX

```

FIG 13B

4 9
33 8
4698
8
9
9
8

FIG 14A

4 9
33 8
4 98
8
9
9
8

FIG 14B

4 9
33 8
4 8
8
9
9
8

FIG 14C

X
X
X
X
N XXX
JNX
N
X
X
X

FIG 15A

X
X
X
X
XXX
X
X
X
X

FIG 15B

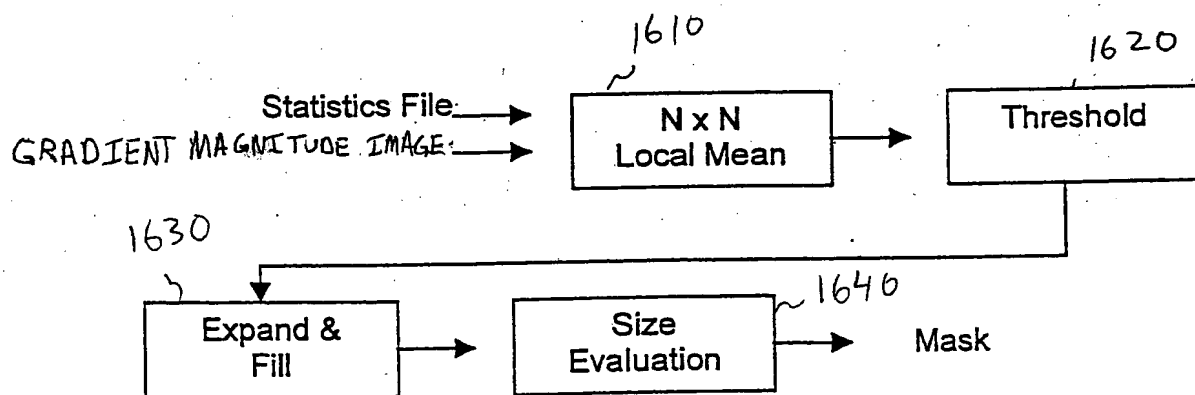


FIG 16

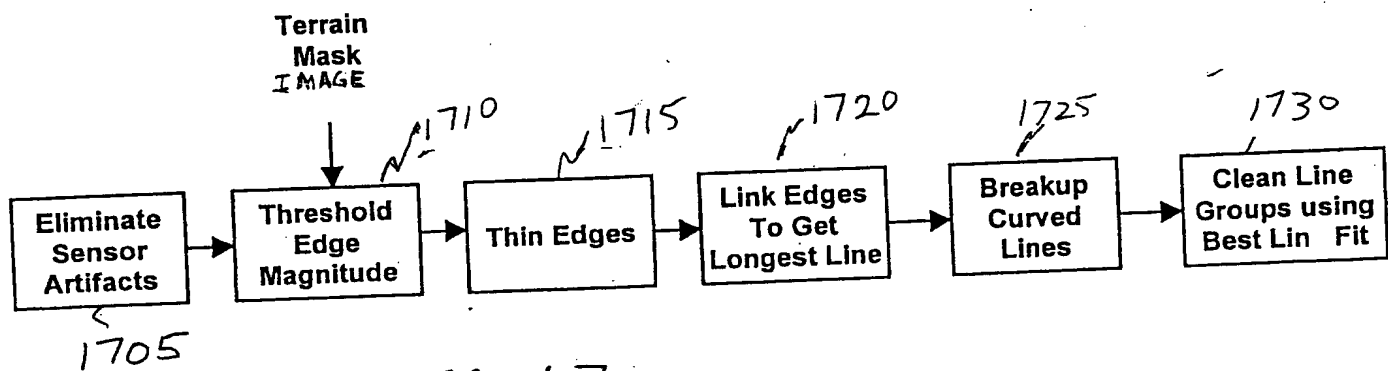
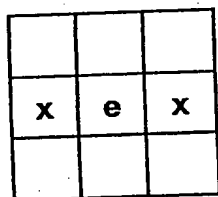
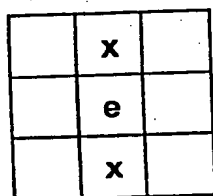


FIG 17



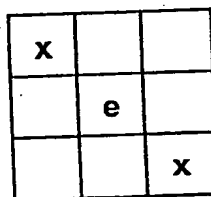
3 and 7

FIG 18A



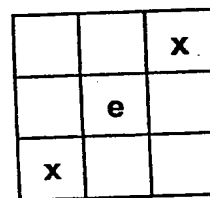
1 and 5

FIG 18B



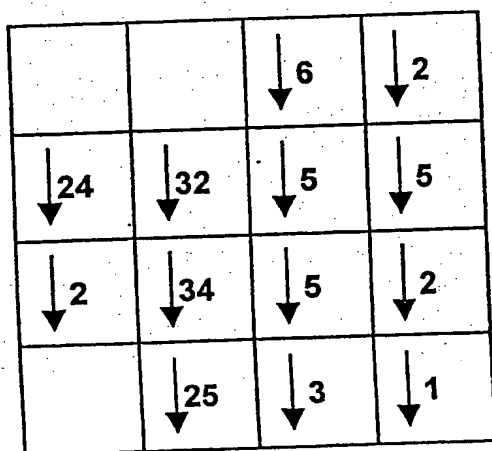
4 and 8

FIG 18C



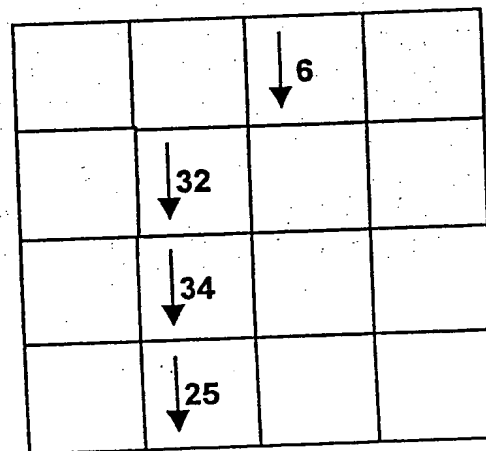
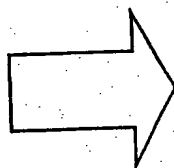
2 and 6

FIG 18D



Edges Directions and Magnitudes

FIG 19A



Thinning Edges

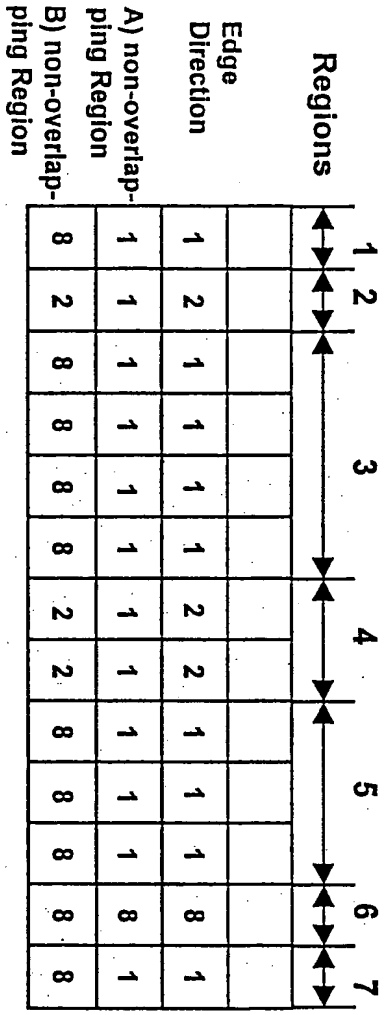
FIG 19B

1	1	1	1	1	1	1	1		

1	2	1	1	1	1	2	2	1	1

No Noise Present
FIG 26A

Noise Present
FIG 26B



- Direction 1 = direction 1 and direction 2
- Direction 2 = direction 2 and direction 3
- Direction 3 = direction 3 and direction 4
- Direction 4 = direction 4 and direction 5
- Direction 5 = direction 5 and direction 6
- Direction 6 = direction 6 and direction 7
- Direction 7 = direction 7 and direction 8
- Direction 8 = direction 8 and direction 1

FIG 20C



FIG 21A

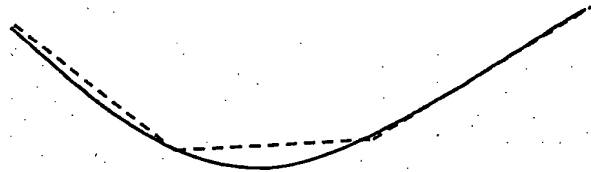


FIG 21B

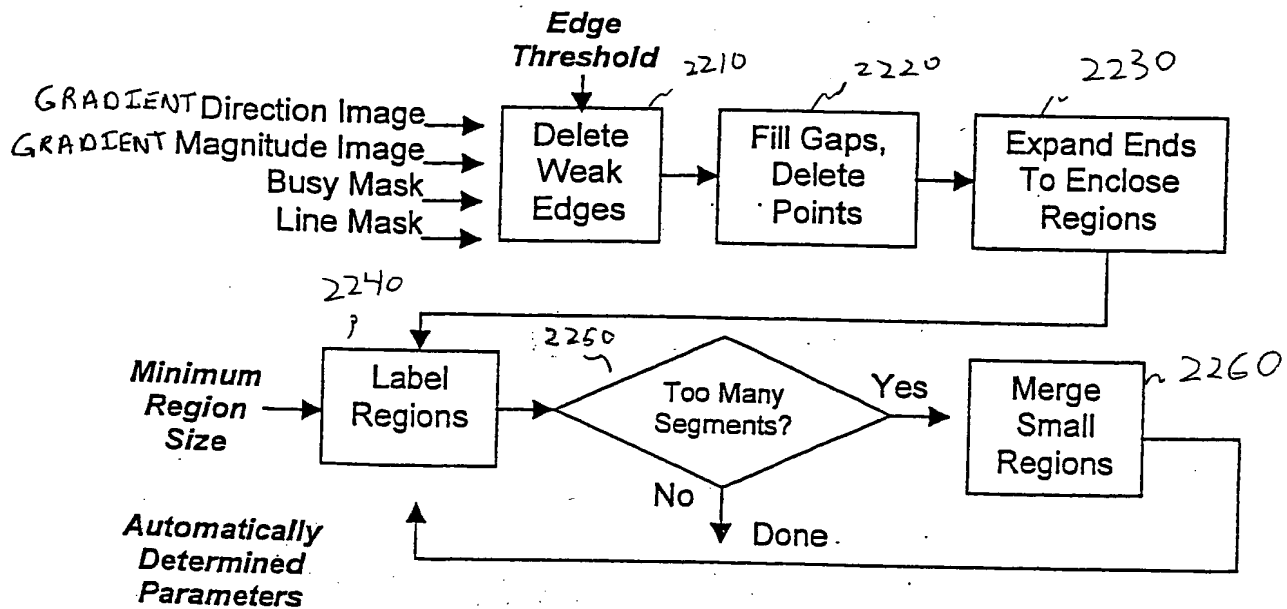


FIG 22

EEO	OOE	OEO	OEO
OCO	OCO	OCO	OCO
OEO	OEO	EEO	OEE

Templates for Vertical Point Gap

C = center pixel, value 1 E = pixel value 1 O = Zero pixel value

EOO	OOE	OOO	OOO
ECE	ECE	ECE	ECE
OOO	OOO	EEO	OOE

Templates for Horizontal Point Gap

FIG 23

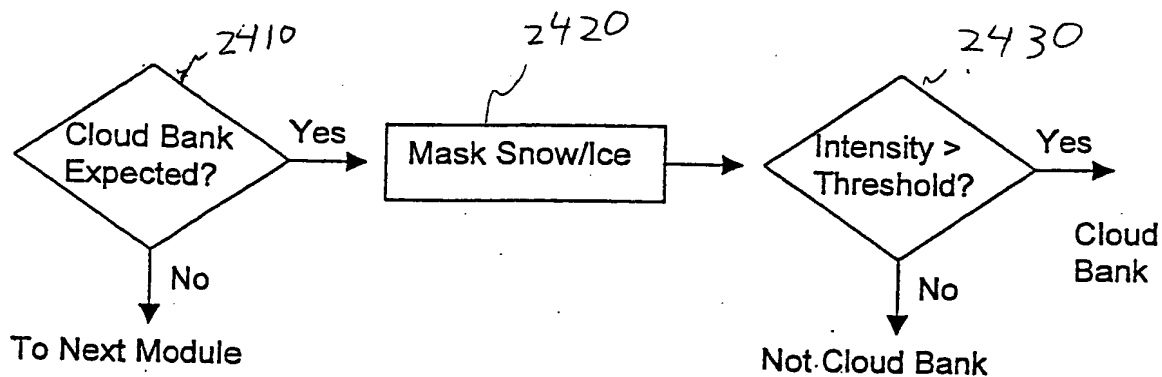


FIG 24

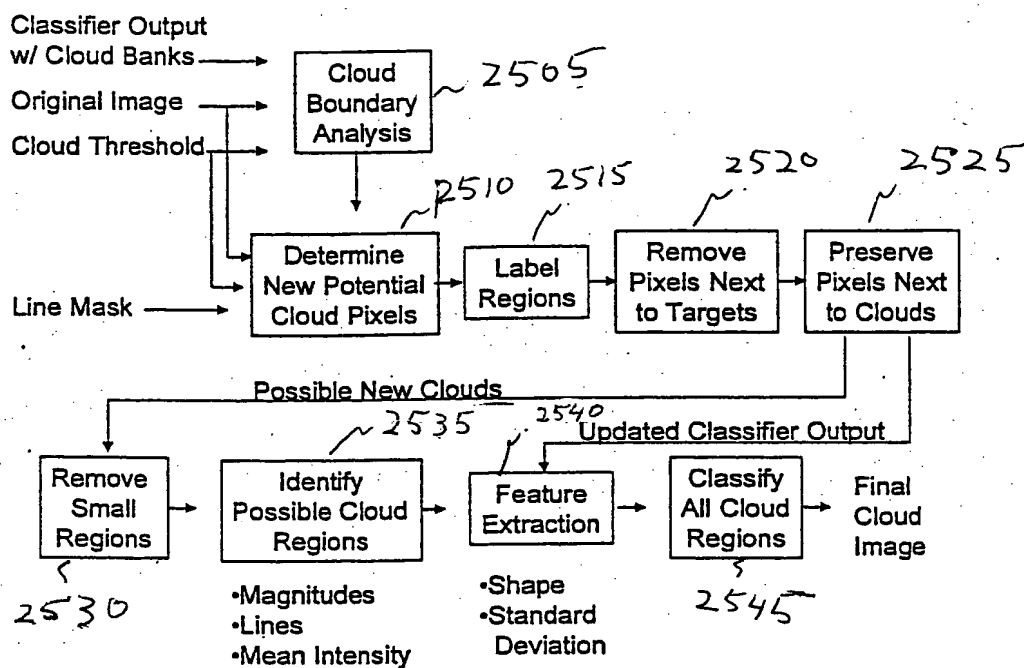


FIG 25

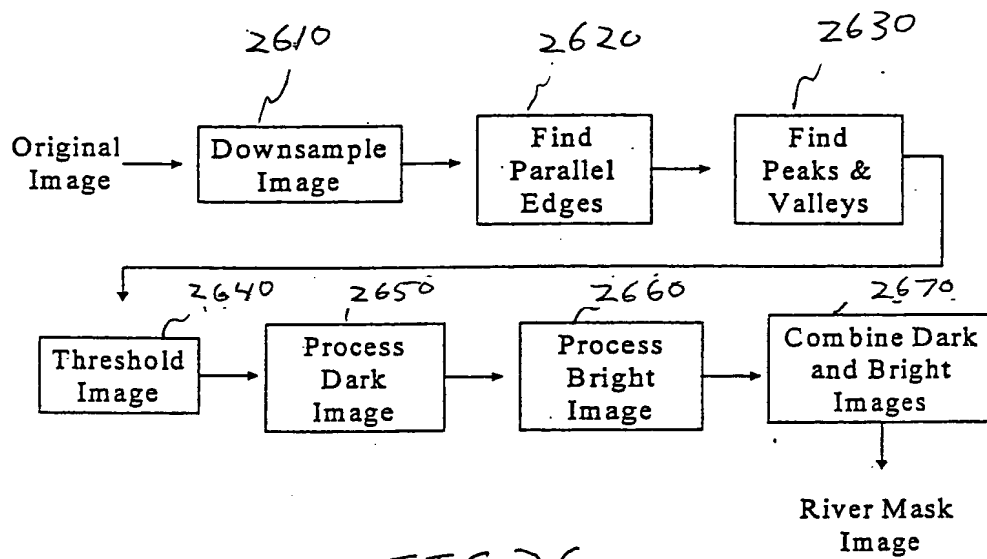


FIG 26

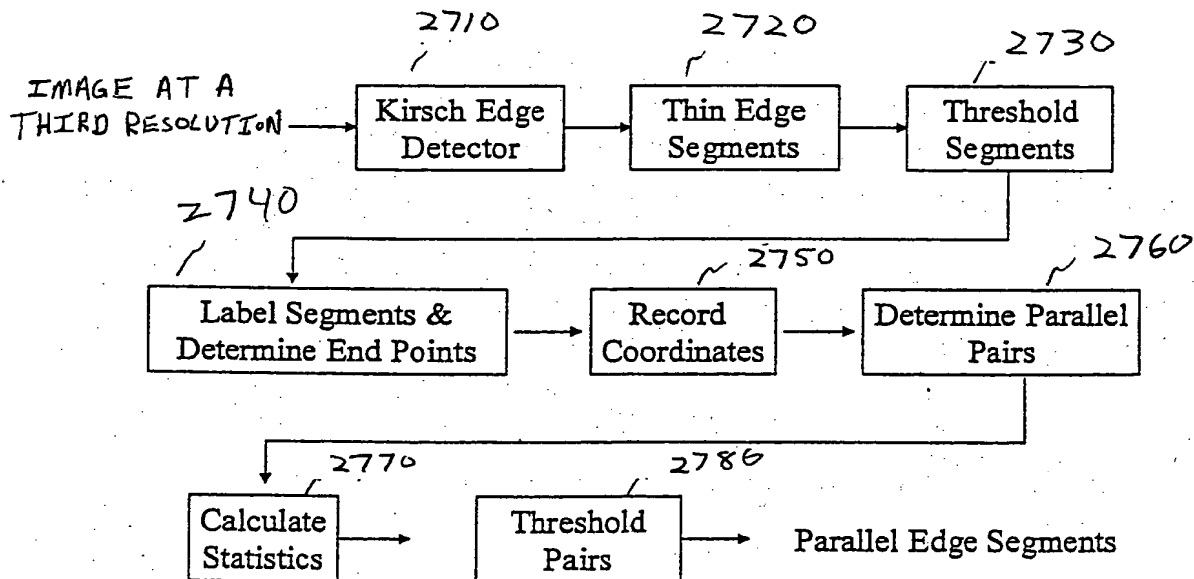
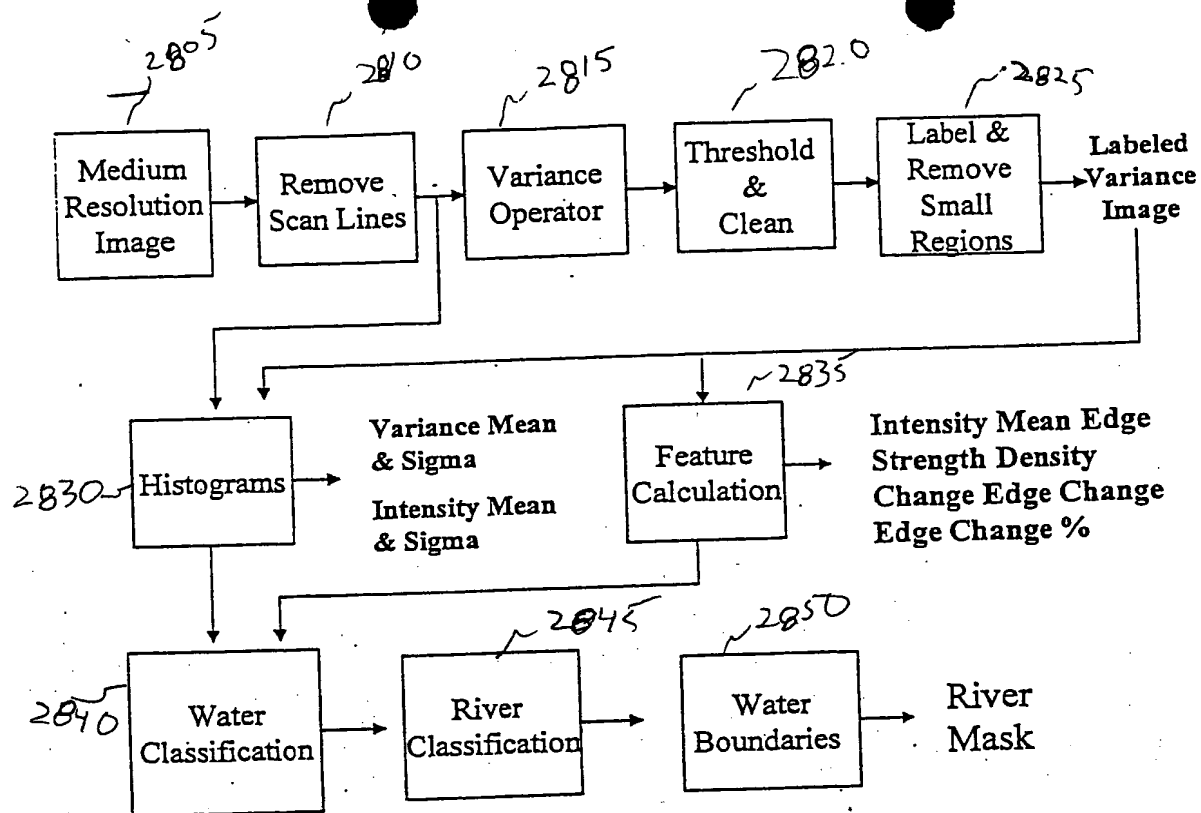


FIG 27



$a_{-1,-1}$	$a_{0,-1}$	$a_{1,-1}$
$a_{-1,0}$	$a_{0,0}$	$a_{1,0}$
$a_{-1,1}$	$a_{0,1}$	$a_{1,1}$

3by3 neighborhood

$$\sigma = \frac{1}{n} \sum_{j=-k}^k \sum_{i=-k}^k (a_{ij} - \mu)^2$$

where

$$\mu = \frac{1}{n} \sum_{i=-k}^k (a_{ij})$$

FIG 29B

For a 3by3 neighborhood $k=1$

FIG 29A

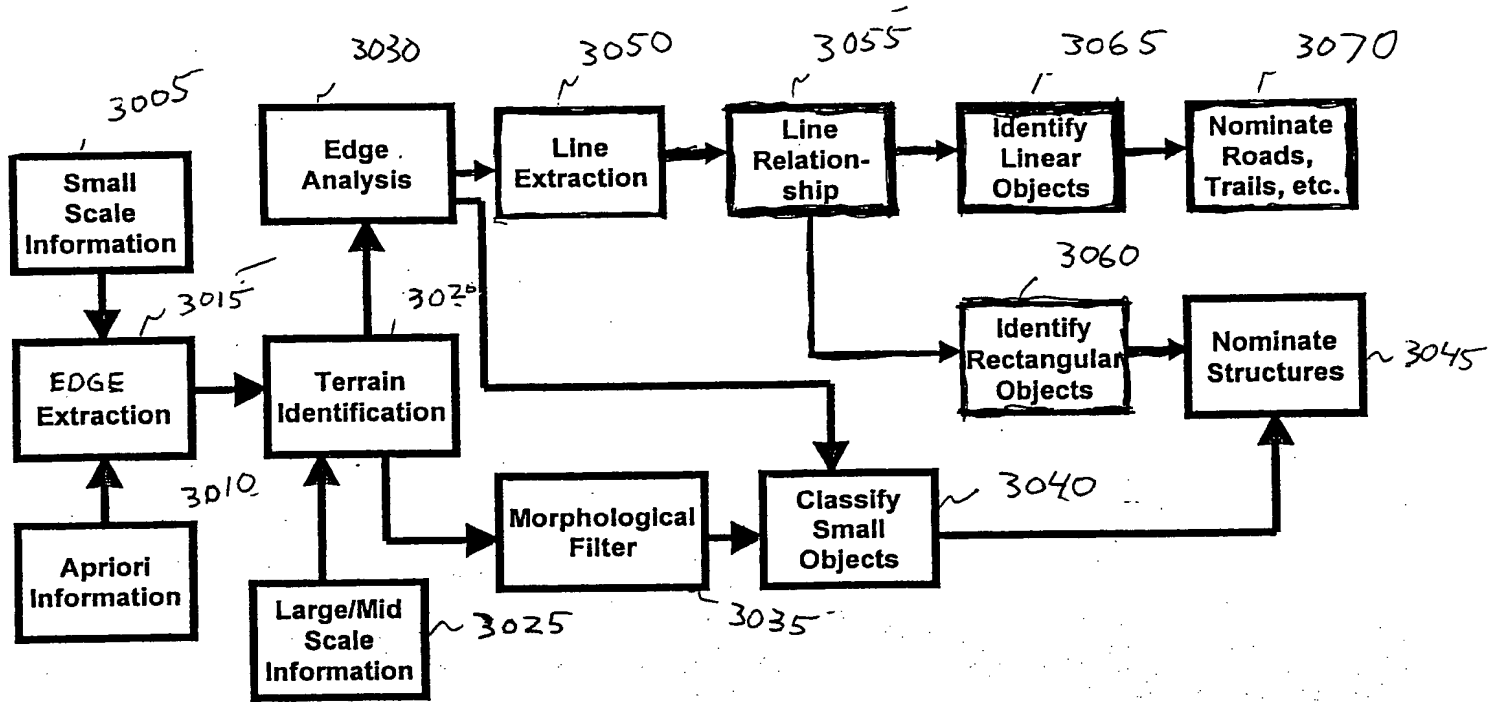


FIG 30

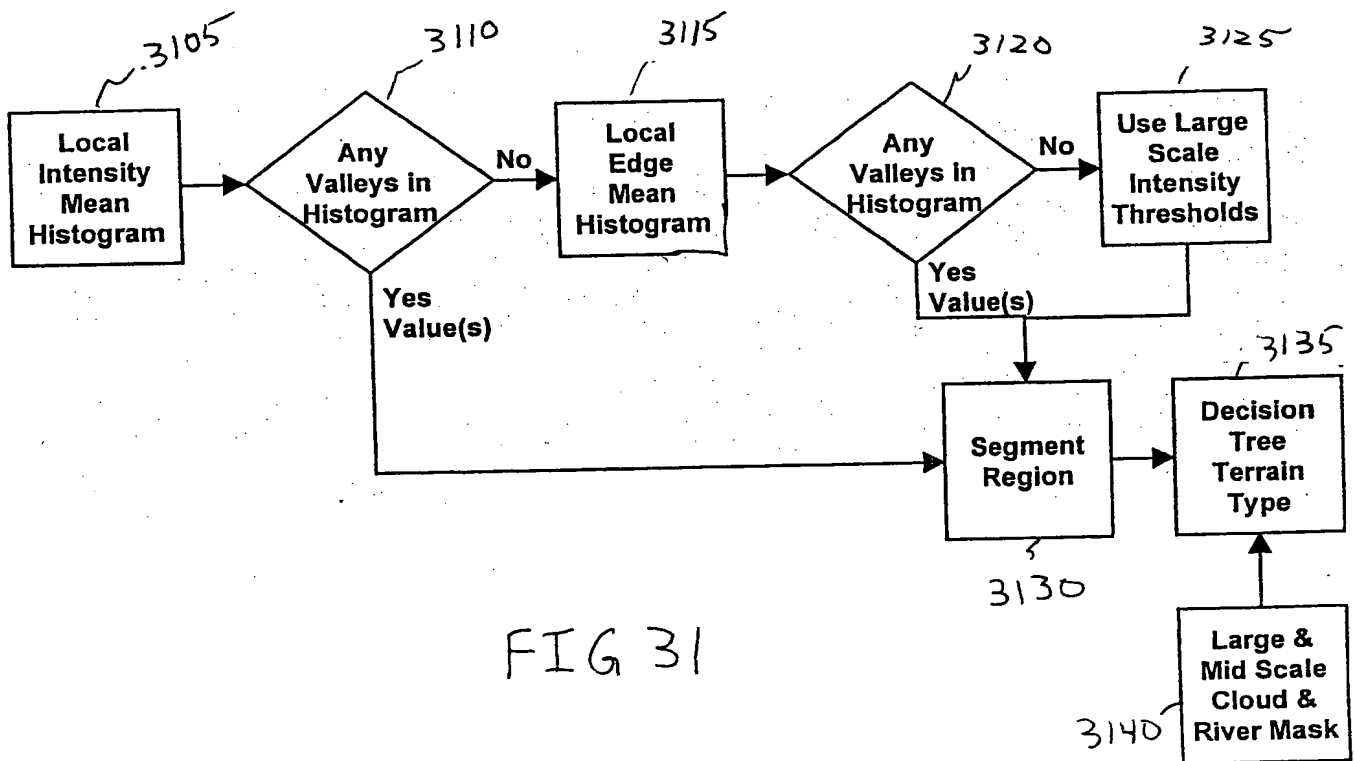


FIG 31

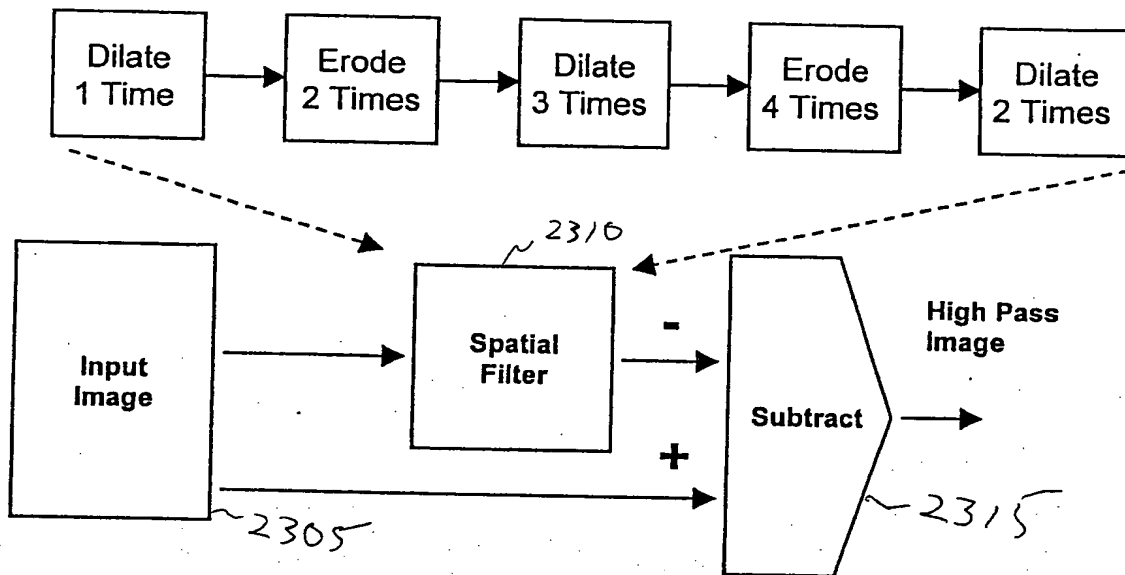


FIG 32

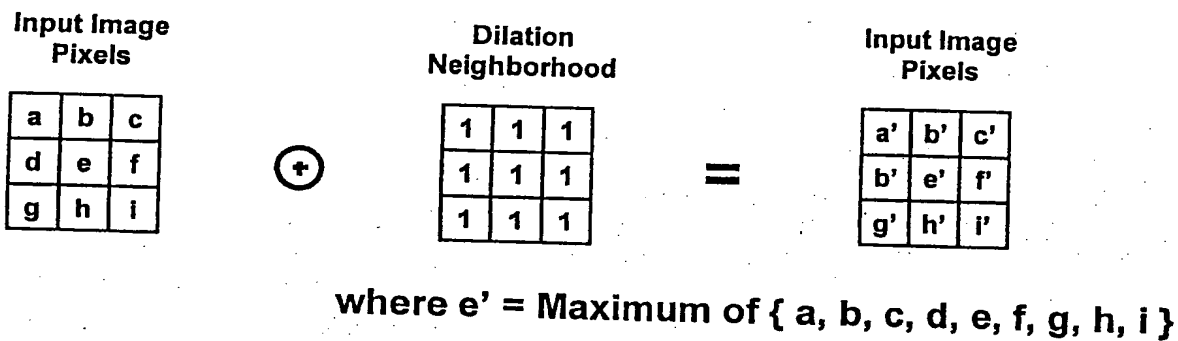


FIG 33A

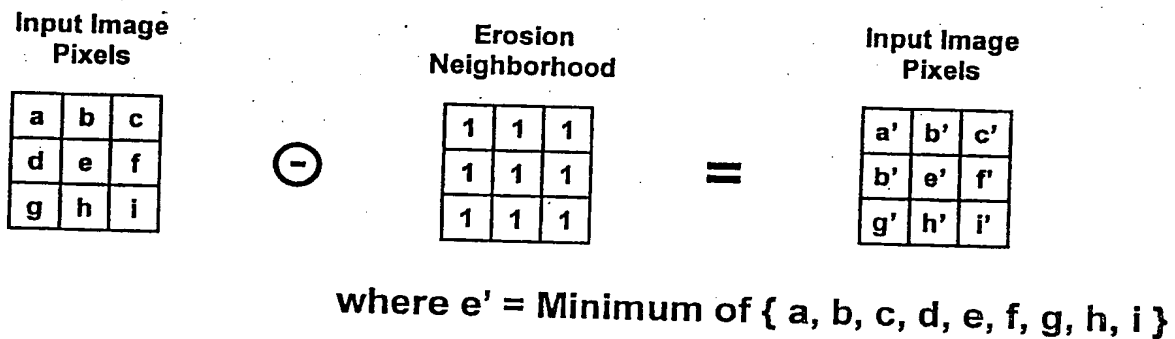


FIG 33B

1 1 1	-1 0 1	0 1 1	-1 -1 0
0 0 0	-1 0 1	-1 0 1	-1 0 1
-1 -1 -1	-1 0 1	-1 -1 0	0 1 1
Horizontal	Vertical	Diagonal 1	Diagonal 2

FIG 34A

	<u>Horizontal</u>		<u>Vertical</u>		<u>Diagonal 1</u>		<u>Diagonal 2</u>	
Gradient Sign	+	-	+	-	+	-	+	-
Direction	1	5	3	7	2	6	4	8

FIG 34B

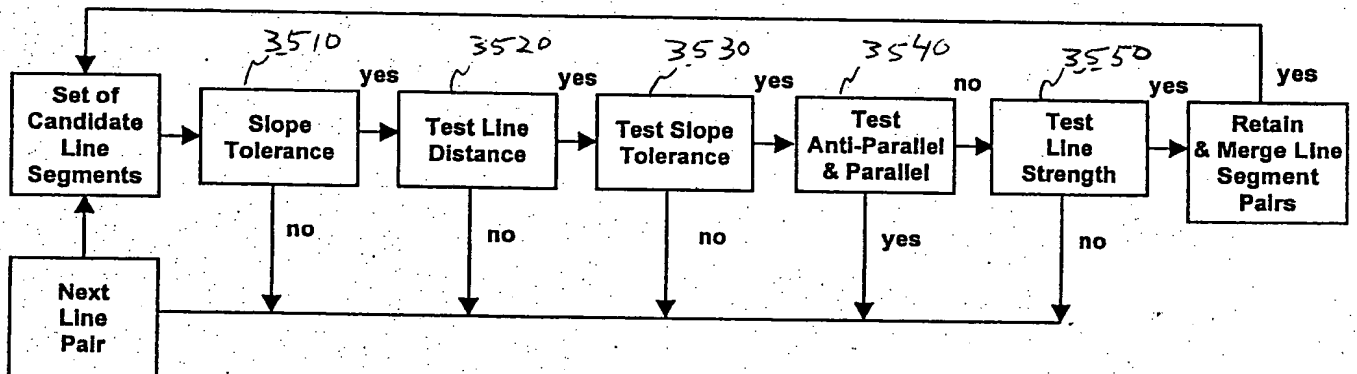


FIG 35

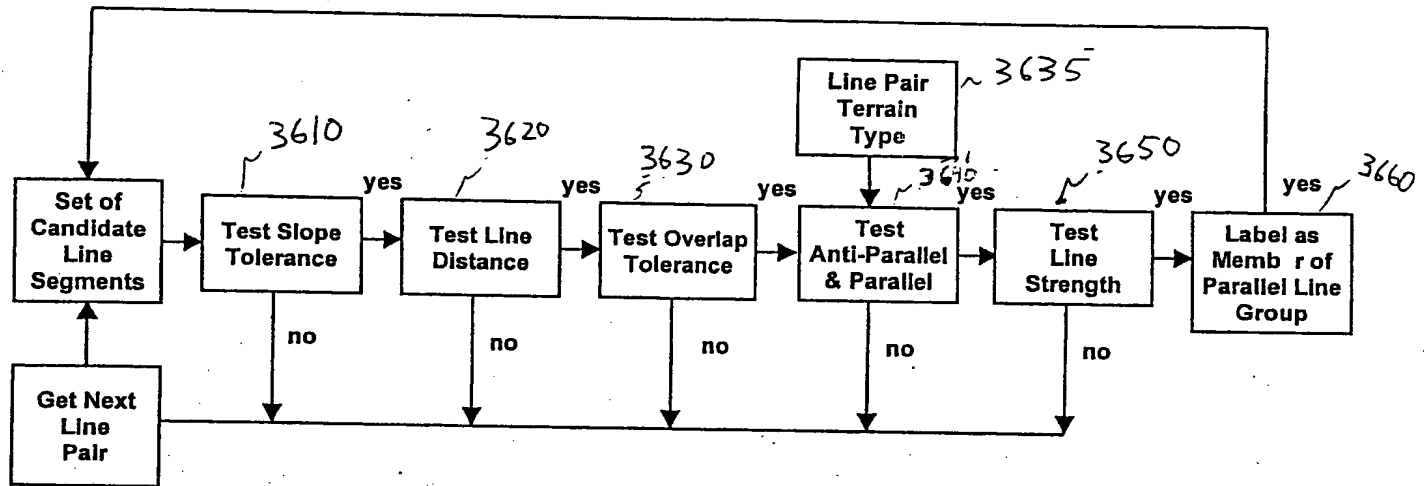


FIG 36

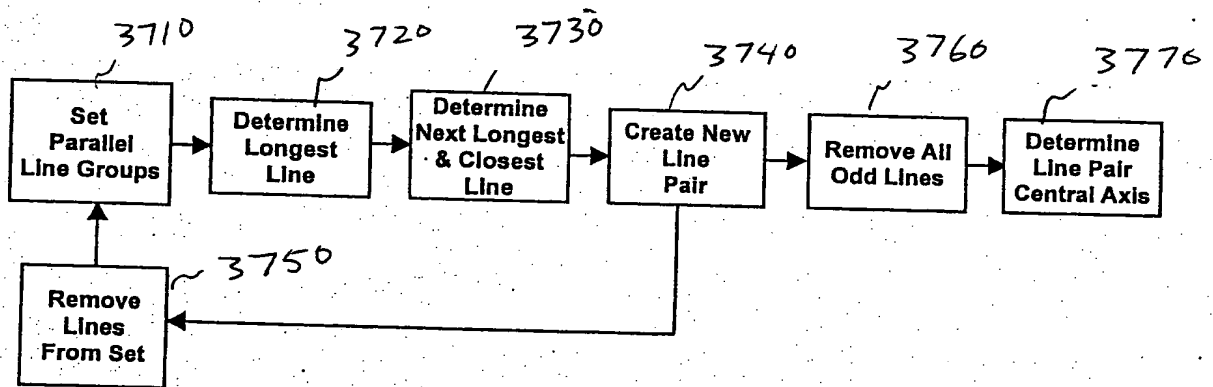


FIG 37

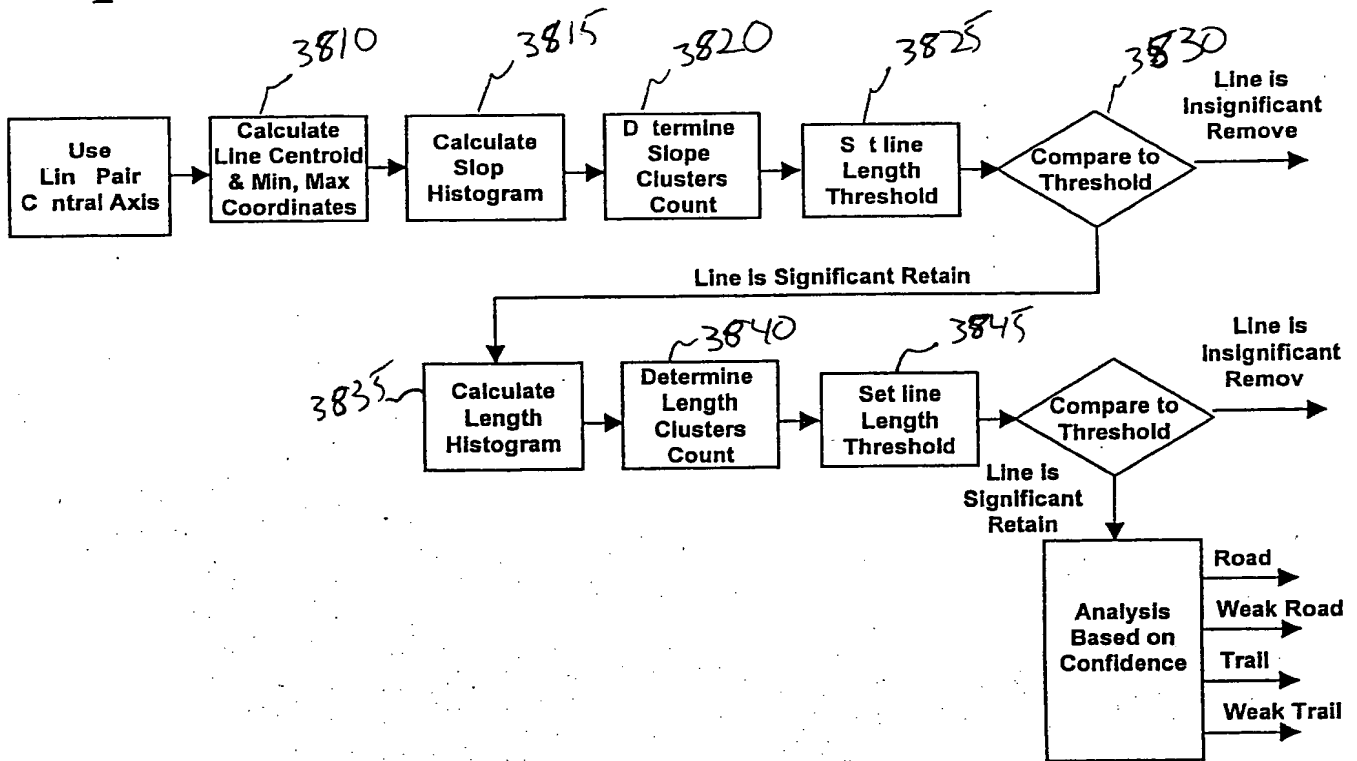


FIG 38

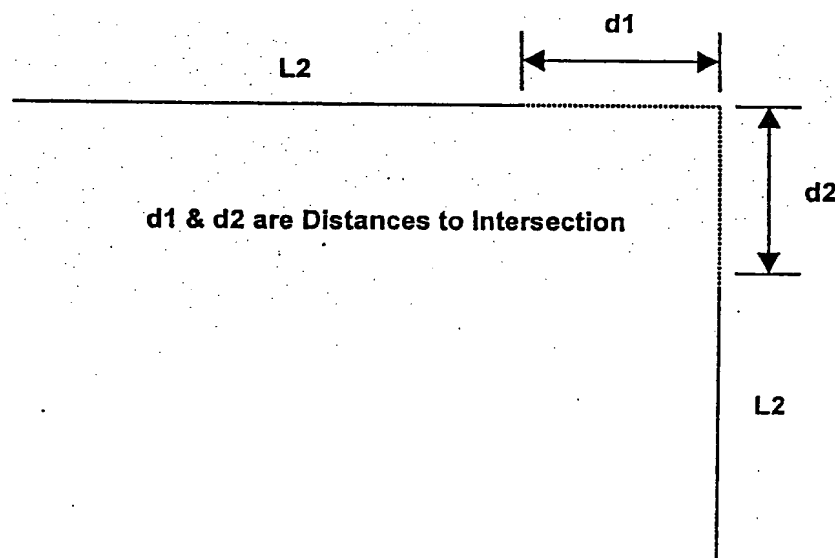
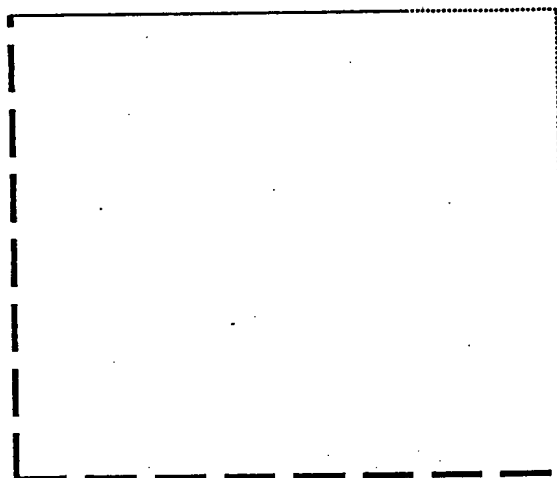


FIG 39



- Detected Line
- Extended Line
- - - - - Reflected Line

FIG 40

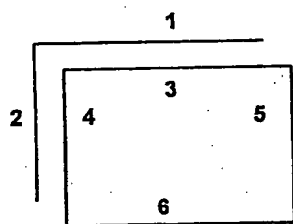


FIG 41A

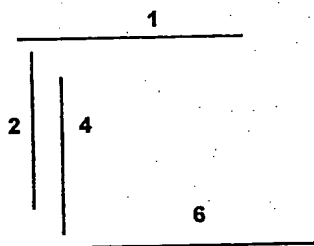


FIG 41B

Reflected and Extended

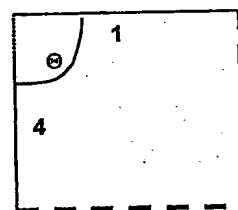


FIG 41C

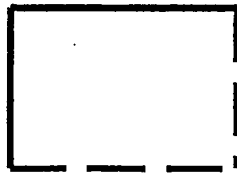


FIG 42A

— Detected Line
 - - - Reflected Line

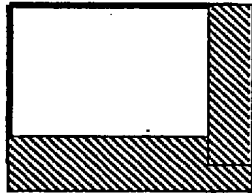


FIG 42B

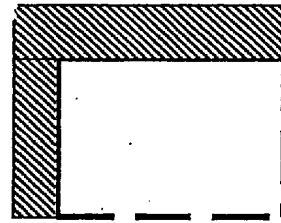


FIG 42C

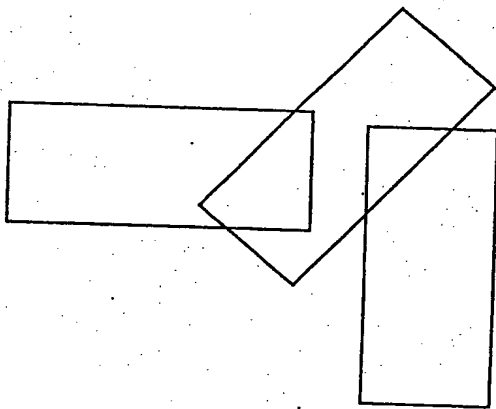


FIG 43A

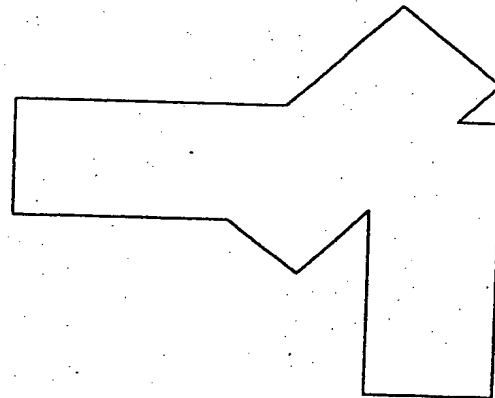


FIG 43B

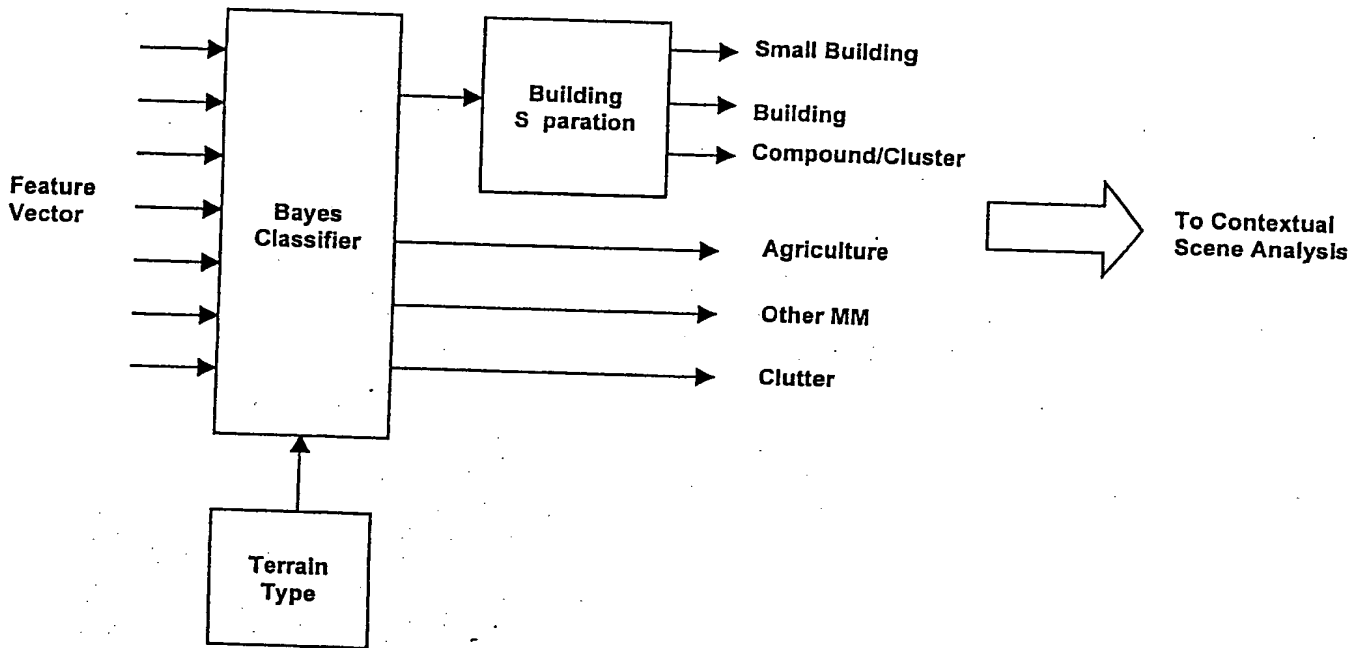


FIG 44

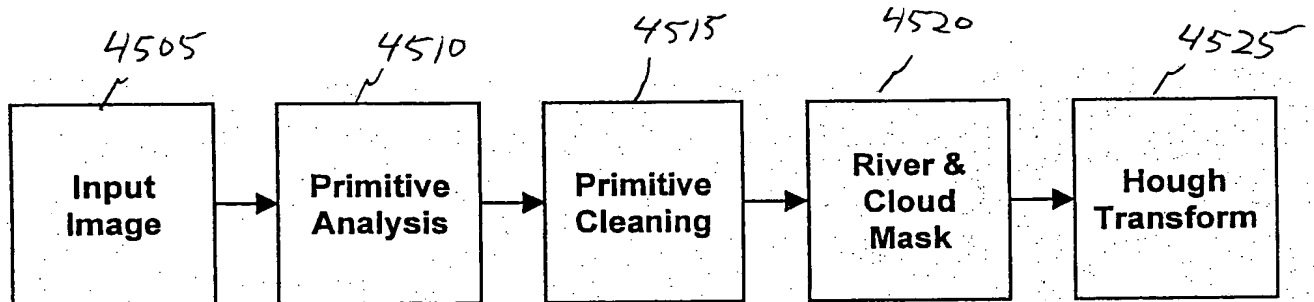


FIG 45

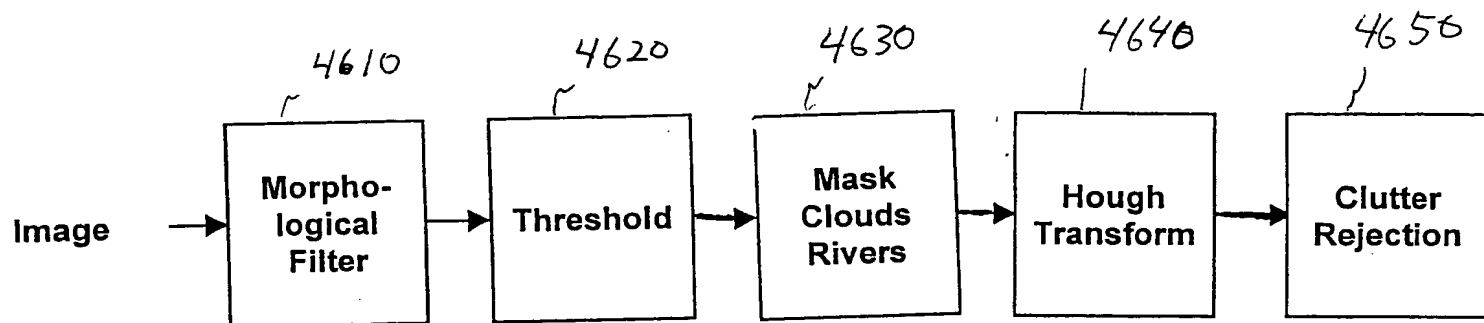


FIG 46

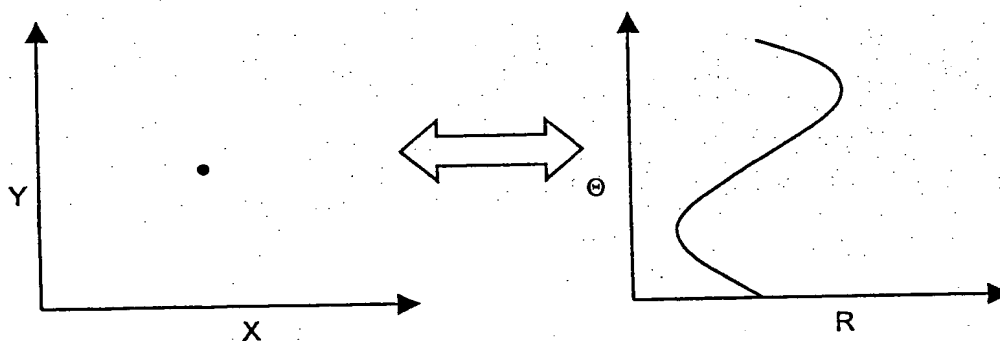


FIG 47A

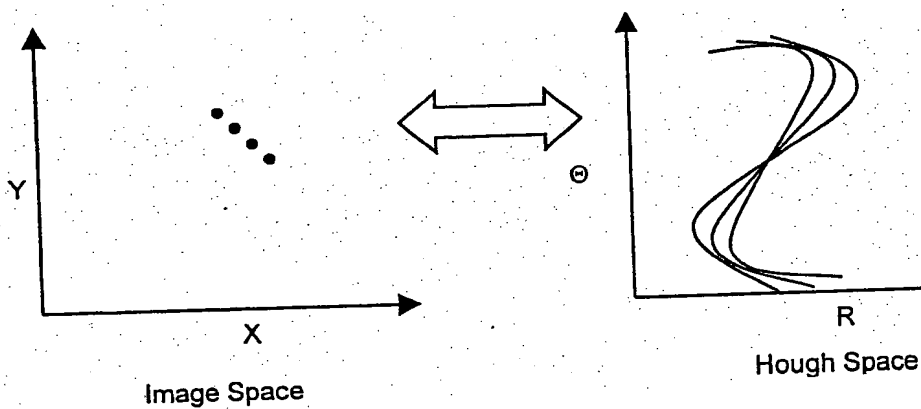


FIG 47B

$$R = x * \cos(\Phi) + y * \sin(\Phi)$$

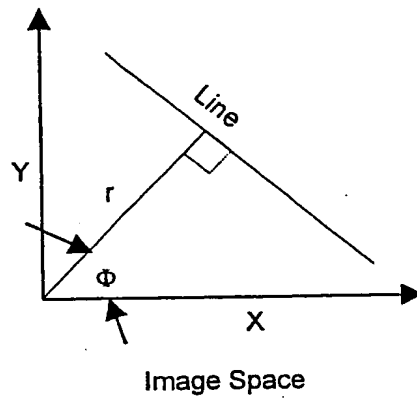


FIG 48

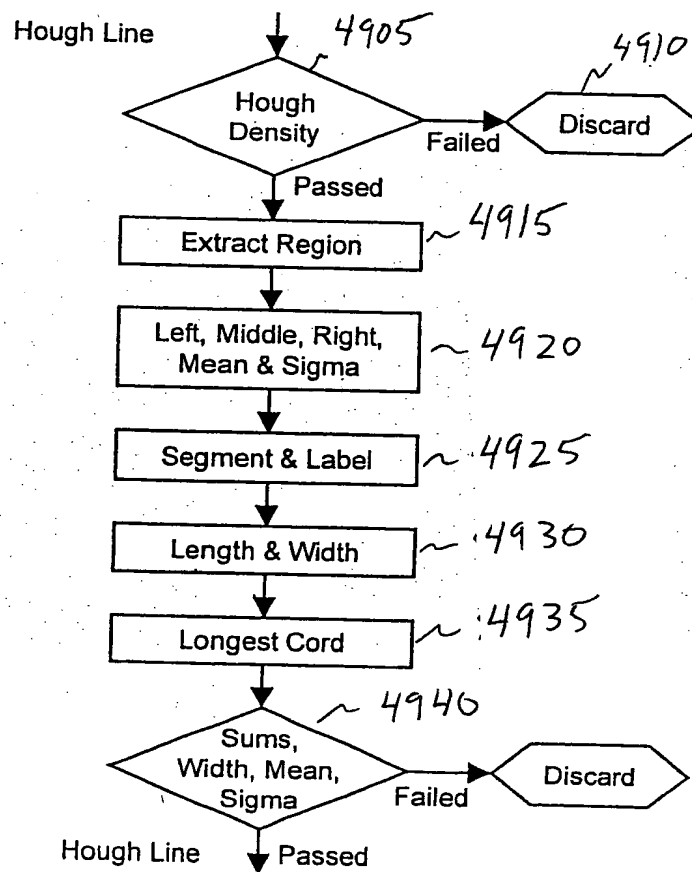


FIG 49

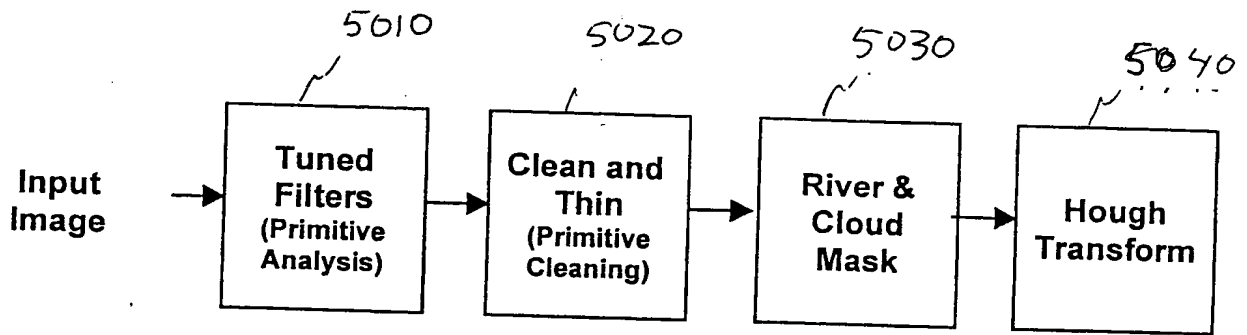


FIG 50

A1	0	B1	0	C1
A2	0	B2	0	C2
A3	0	B3	0	C3
A4	0	B4	0	C4
A5	0	B5	0	C5
A6	0	B6	0	C6
A7	0	B7	0	C7
A8	0	B8	0	C8
A9	0	B9	0	C9
A10	0	B10	0	C10
A11	0	B11	0	C11
A12	0	B12	0	C12
A13	0	B13	0	C13
A14	0	B14	0	C14
A15	0	B15	0	C15

$$B_8 = 2 \times \sum_{i=1}^{15} B_i - \left(\sum_{i=1}^{15} A_i + \sum_{i=1}^{15} C_i \right)$$

FIG 51

A1	A2	A3	A4	A5
A16	B1	B2	B3	A6
A15	B4	B5	B6	A7
A14	B7	B8	B9	A8
A13	A12	A11	A10	A9

FIG 52

	x	
	x	x

	x	x
	x	x

x	x	x
	x	x

x	x	x
x	x	x

x	x	x
x	x	x
		x

x	x	x
x	x	x
	x	x

	x	
x	x	x

x		
x	x	
	x	x

FIG 53

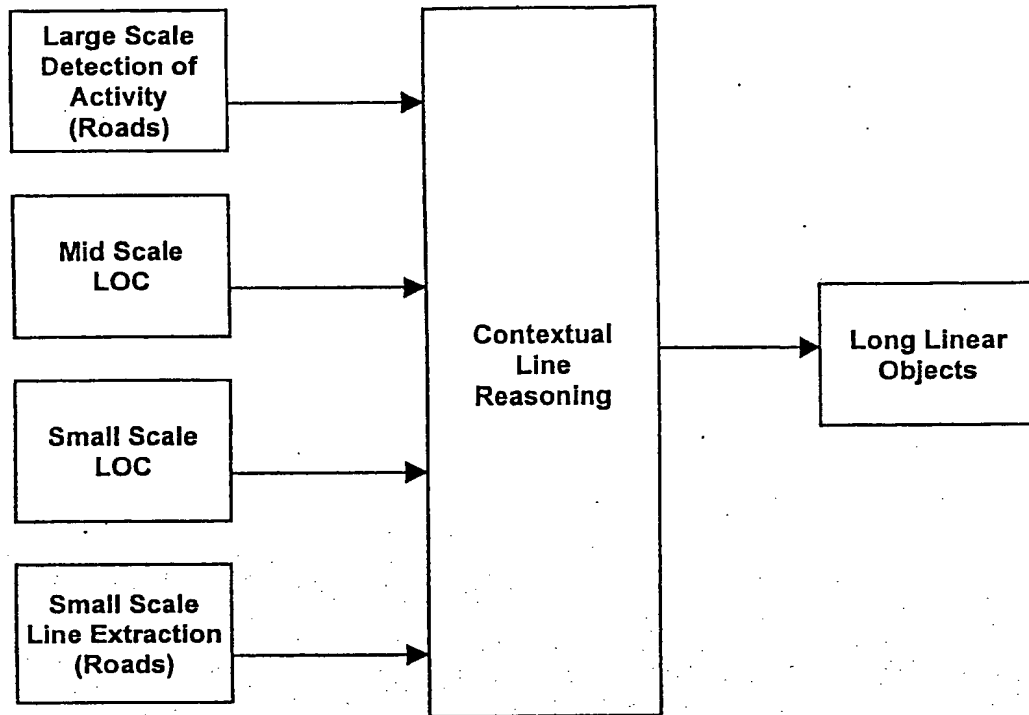


FIG 56

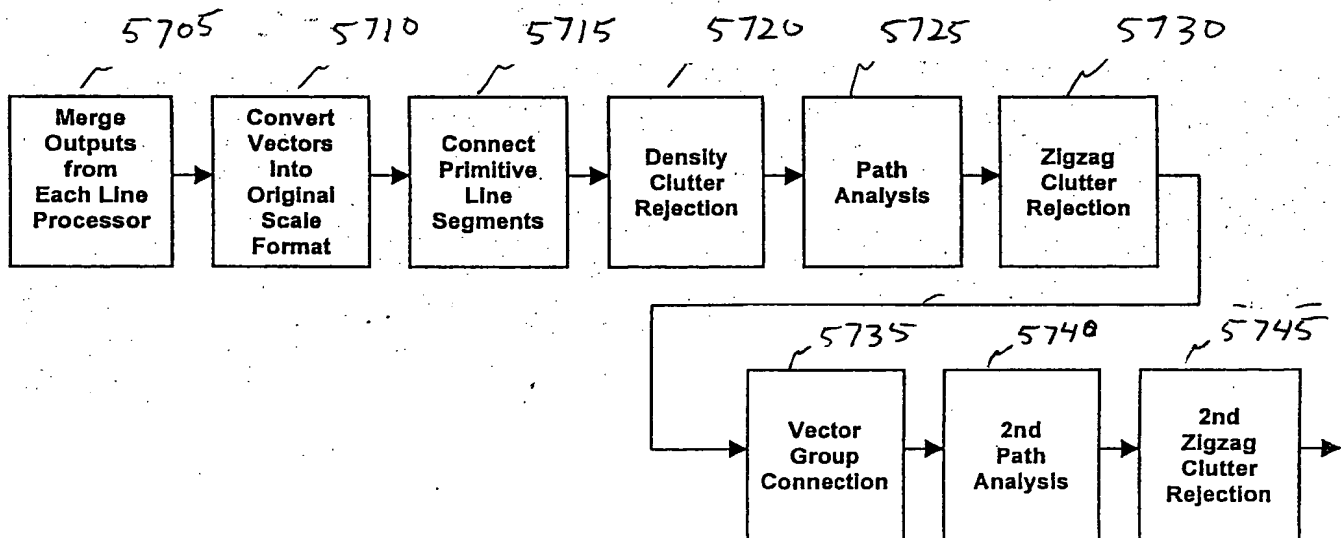


FIG 57

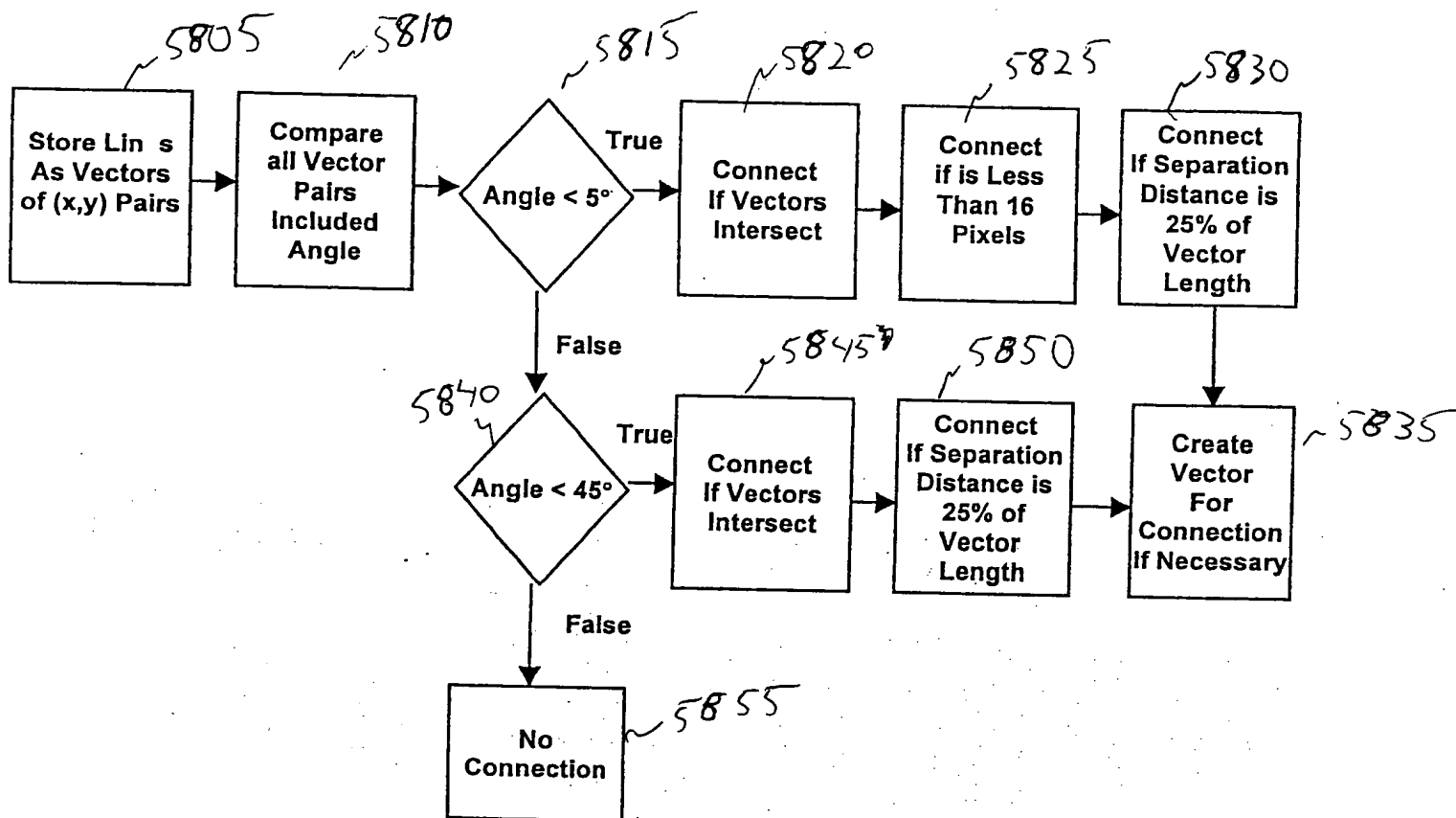


FIG 58

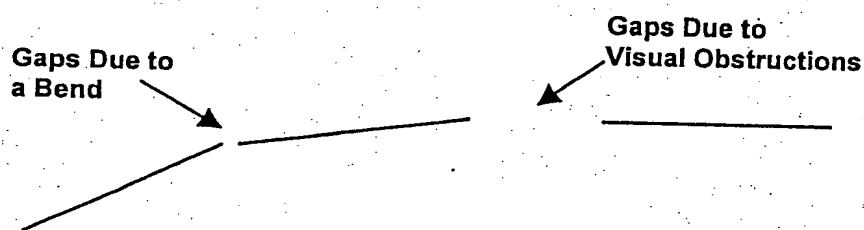


FIG 59A

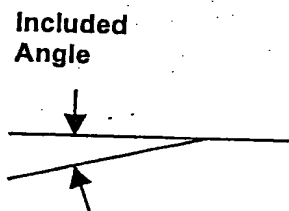


FIG 59B

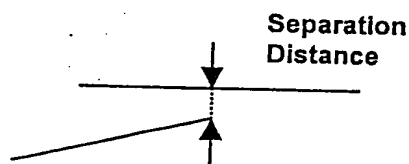


FIG 59C

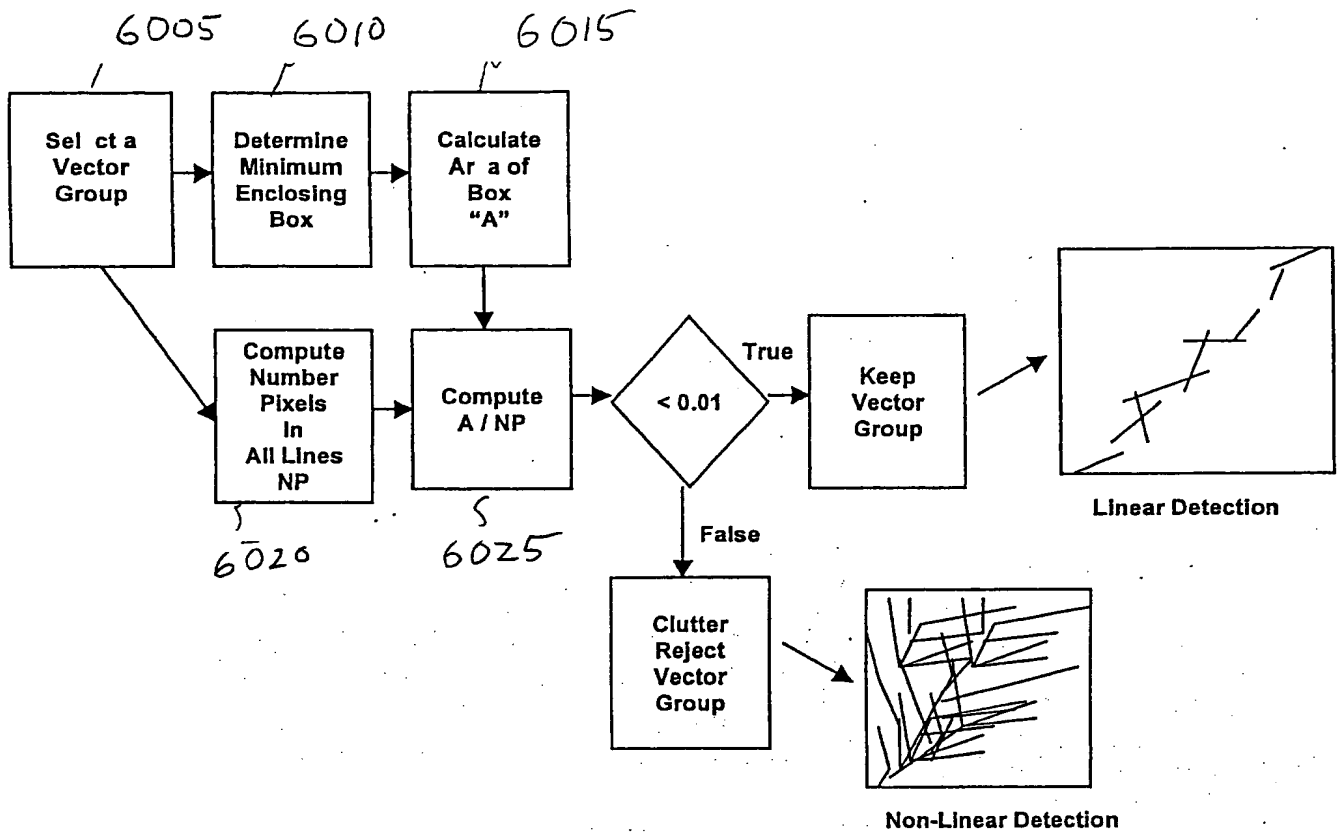


FIG 60

$M^1 = \|m_{ij}^1\|$ Where m_{ij}^1 is the direct distance

between node i and j in pixels

$M^2 = \|m_{ij}^2\|$ Where m_{ij}^2 is the direct distance

between node i and j in pixels using a most one intermediate node

$$M^2 = M^1 \otimes M^1$$

$$M^4 = M^2 \otimes M^2$$

In general the following is true

$$M^{n+m} = M^n \otimes M^m$$

When $M' \equiv M'^{\alpha}$ where α is a positive number

all paths are connect

FIG 61

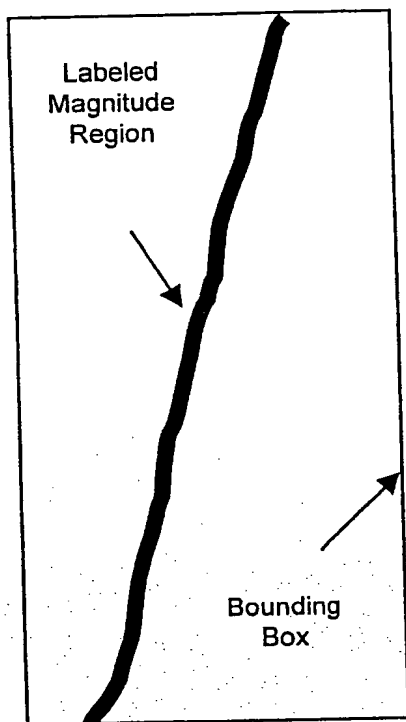


FIG 54

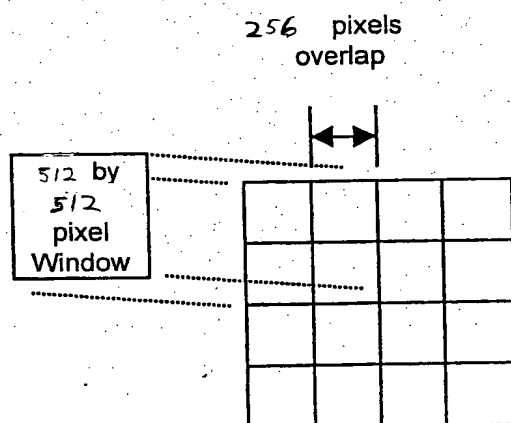
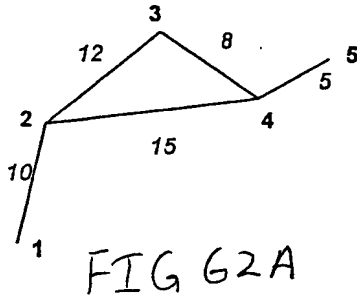


FIG 55



$$M^1 = \begin{bmatrix} 0 & 10 & 0 & 0 & 0 \\ x & 0 & 12 & 15 & 0 \\ x & x & 0 & 8 & 0 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

FIG 62B

$$M^2 = \begin{bmatrix} 0 & 10 & 22 & 25 & 0 \\ x & 0 & 12 & 15 & 20 \\ x & x & 0 & 8 & 13 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

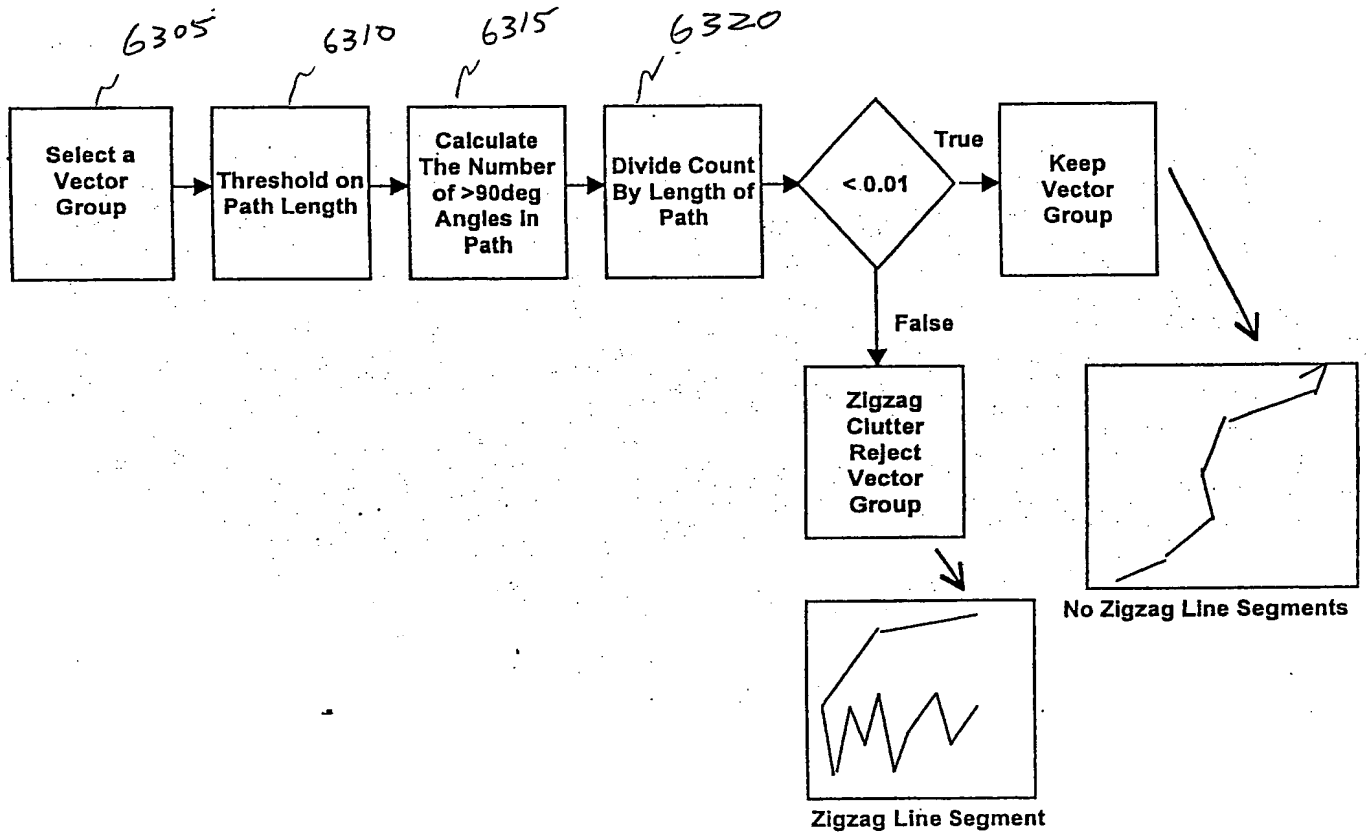
FIG 62C

$$M^3 = \begin{bmatrix} 0 & 10 & 22 & 25 & 30 \\ x & 0 & 12 & 15 & 20 \\ x & x & 0 & 8 & 13 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

FIG 62D

$$M^3 = M^4$$

FIG 62E



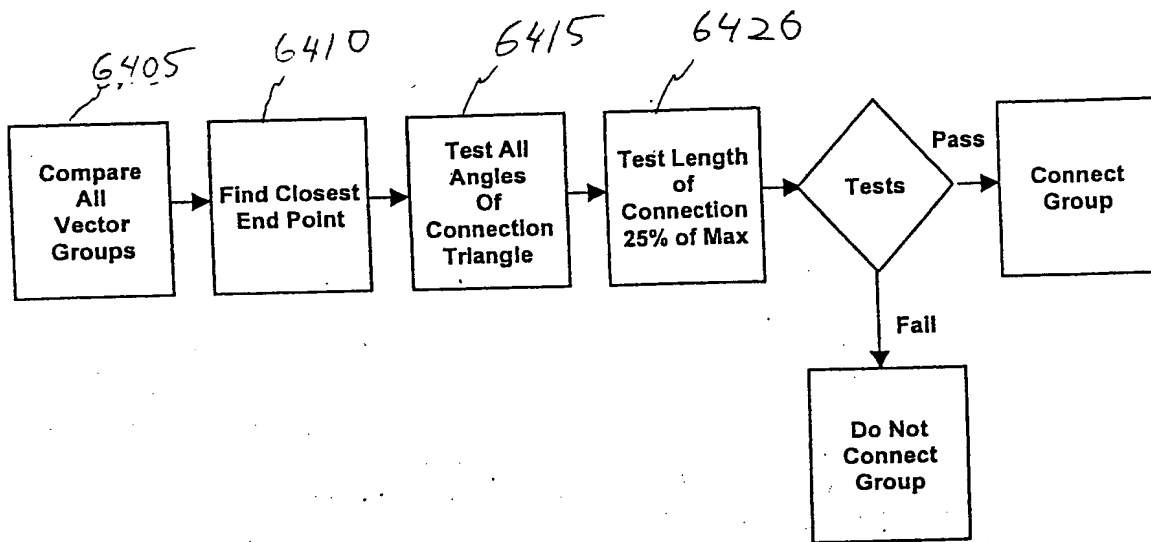


FIG 64

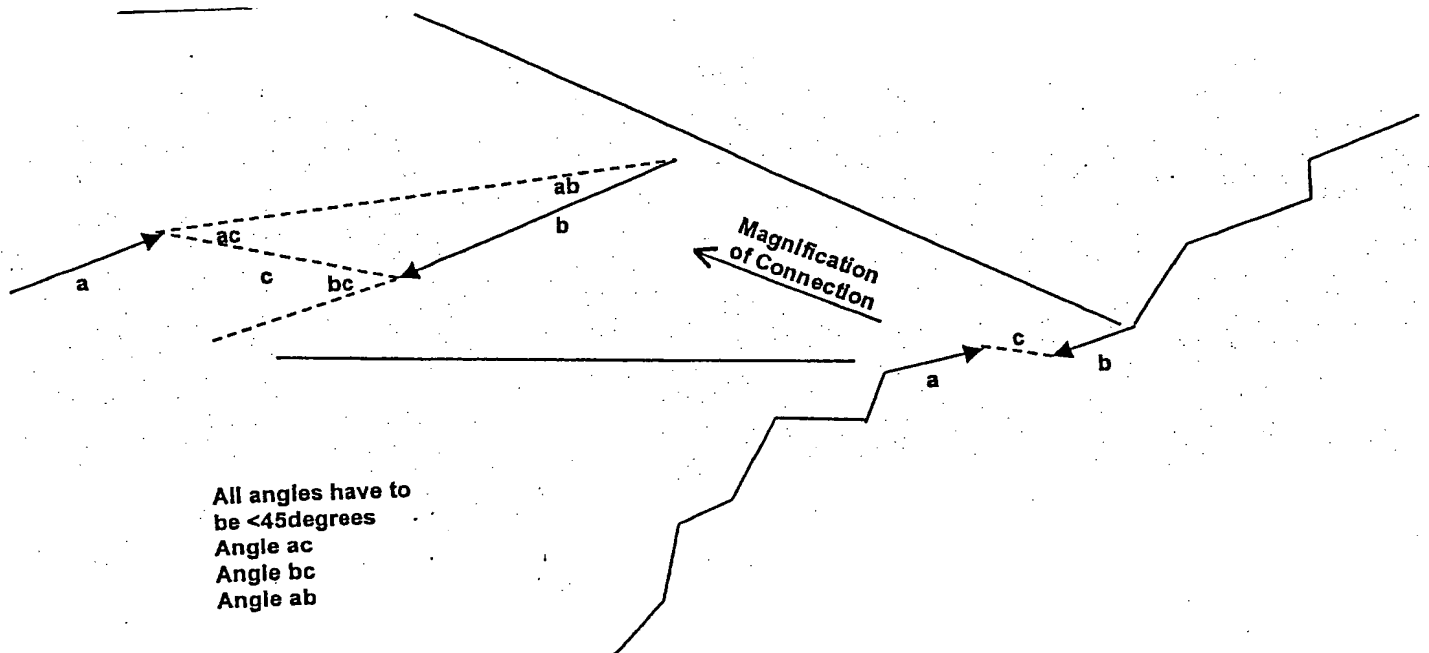


FIG 65

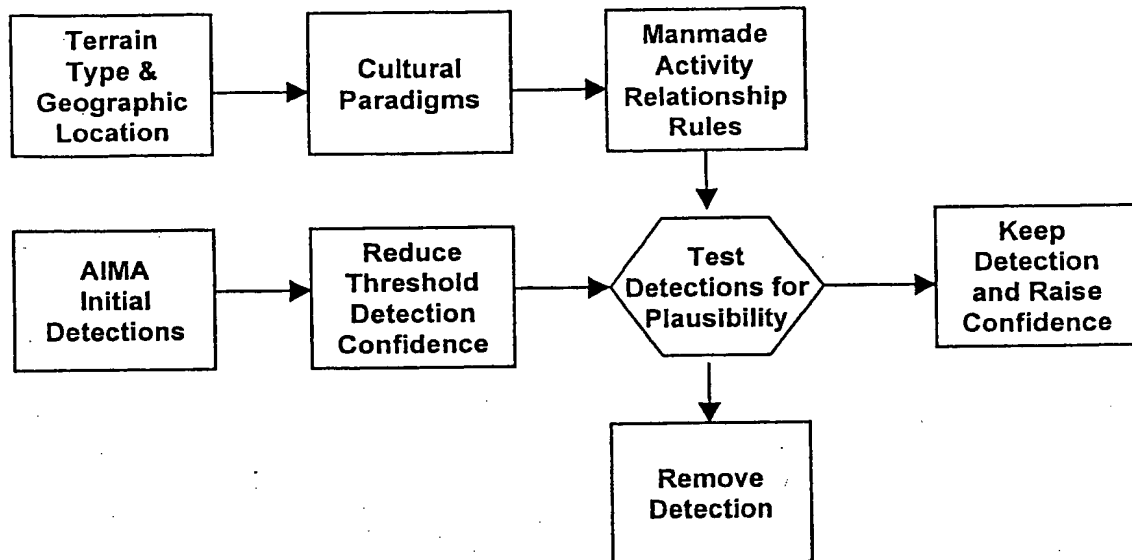


FIG 66